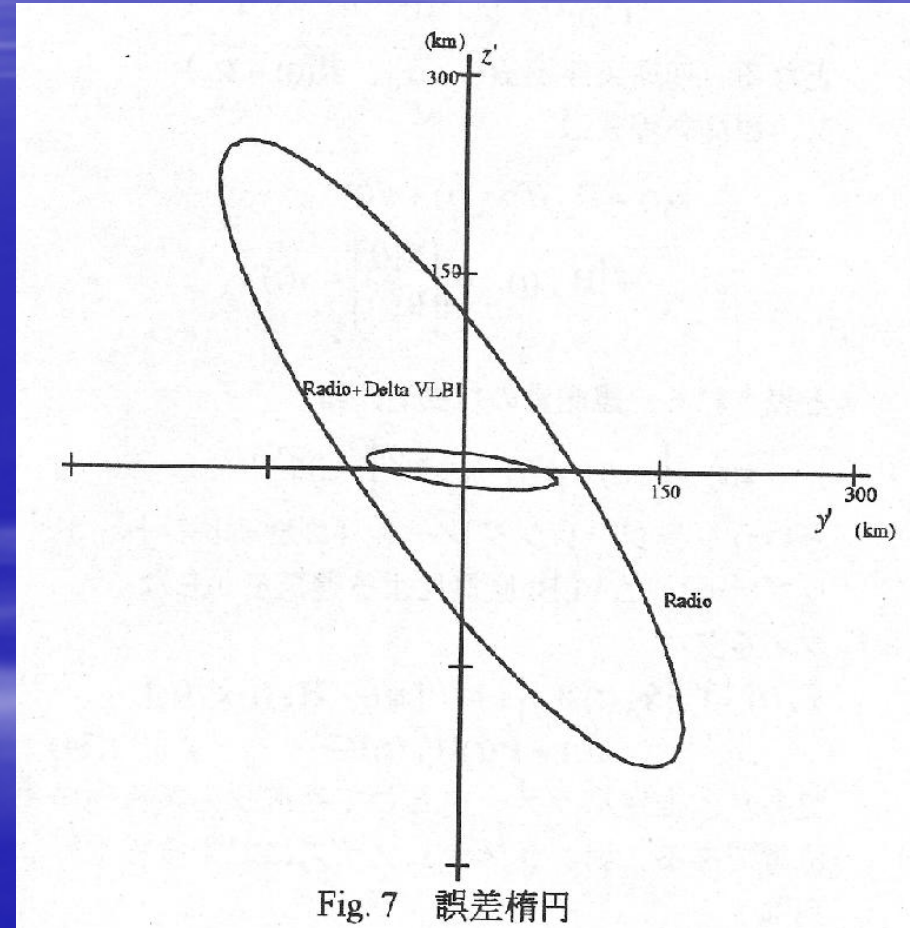
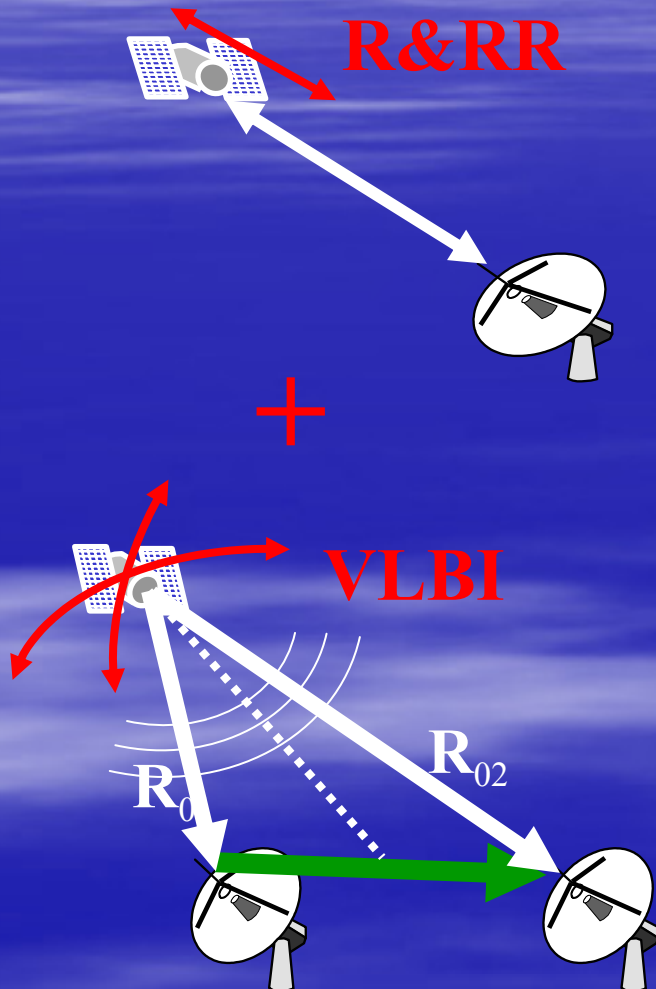


VLBI Application for Spacecraft Navigation

Mamoru Sekido, Ryuichi Ichikawa, Hiroshi Takeuchi,
Yasuhiro Koyama, Eiji Kawai, Tetsuro Kondo (NICT, Japan),
Makoto Yoshikawa, Nanako Mochizuki, Yasuhiro Murata,
Takaji Kato, Tsutomu Ichikawa,
Hisashi Hirabayashi (ISAS/JAXA, Japan),
Takafumi Ohnishi (Fujitsu Co. Ltd., Japan),
Fuyuhiko Kikuchi(NAOJ),
Kazuhiro Takashima(GSI, Japan),
Kenta Fujisawa, (Yamaguchi Univ., Japan),
Hiroshi Takaba (Gifu Univ., Japan),
Kazuo Sorai(Hokkaido Univ., Japan),
Wayne Cannon, Sasha Novikov (York Univ., Canada),
Mario Berube (NRCan, Canada)

Spacecraft Navigation

R&RR + VLBI

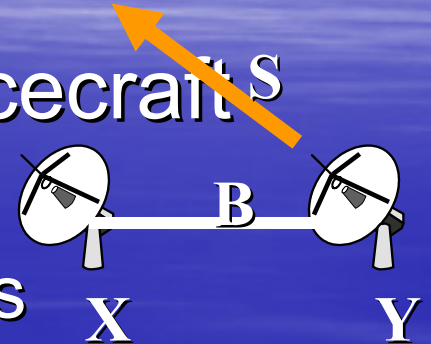


Outline



- What is difference? VLBI for Spacecraft S

- Observation Equation
- Curved wave front = Parallax effects

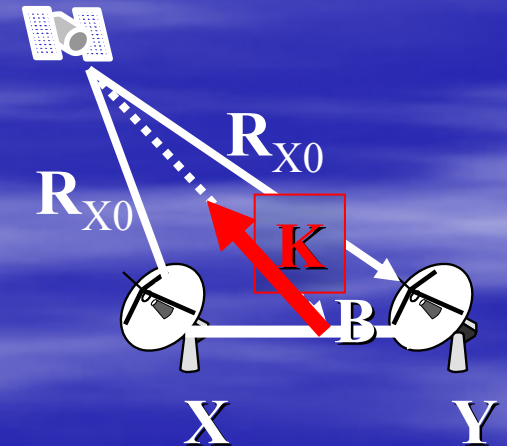


- Data Acquisition Terminal

- K5/VSSP: Disk-Based system
+ Software Correlator

- Observables & Delta VLBI

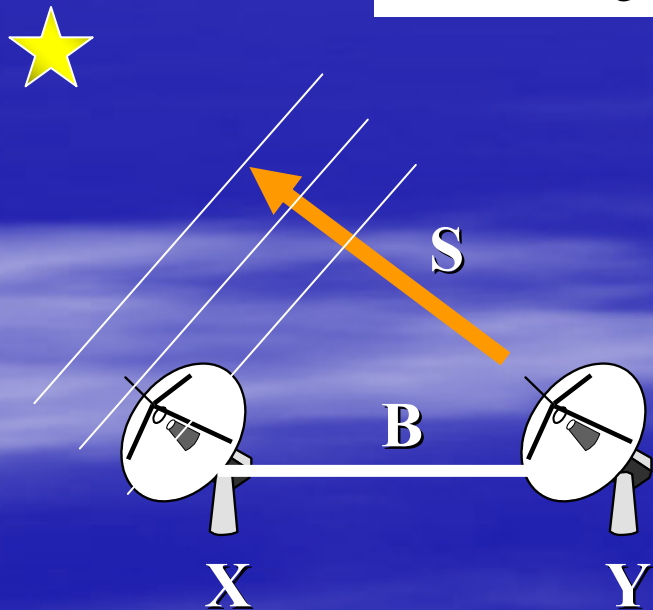
- Group Delay
- Phase Delay



VLBI delay model for finite distance radio source

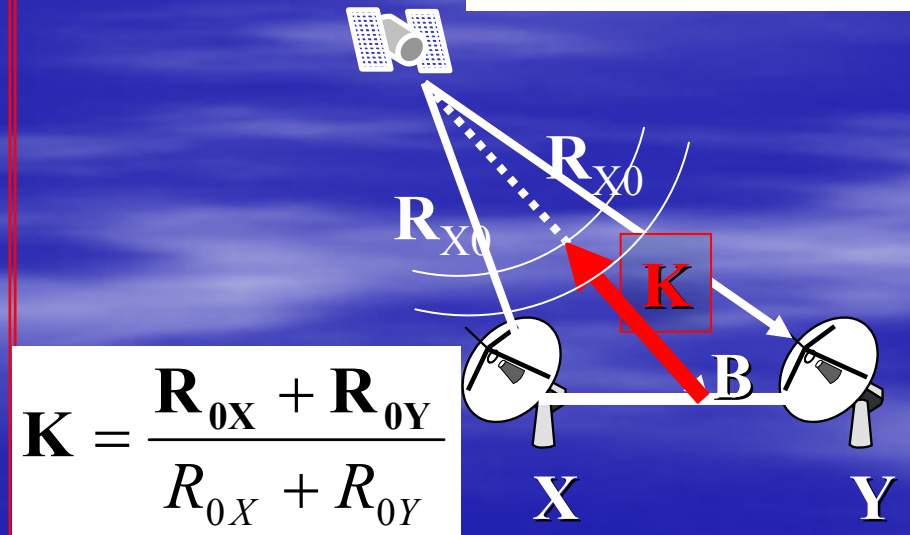
Standard VLBI

$$\mathbf{B} = \mathbf{X} - \mathbf{Y}$$
$$\tau = -\frac{\mathbf{B} \cdot \mathbf{S}}{c}$$



VLBI for finite distance radio source

$$\tau = -\frac{\mathbf{B} \cdot \mathbf{K}}{c}$$



$$\mathbf{K} = \frac{\mathbf{R}_{0X} + \mathbf{R}_{0Y}}{R_{0X} + R_{0Y}}$$

(Fukuhima 1993 A&A)

Relativistic VLBI delay model for finite distance radio source

CONSENSUS MODEL (M.Eubanks 1991)

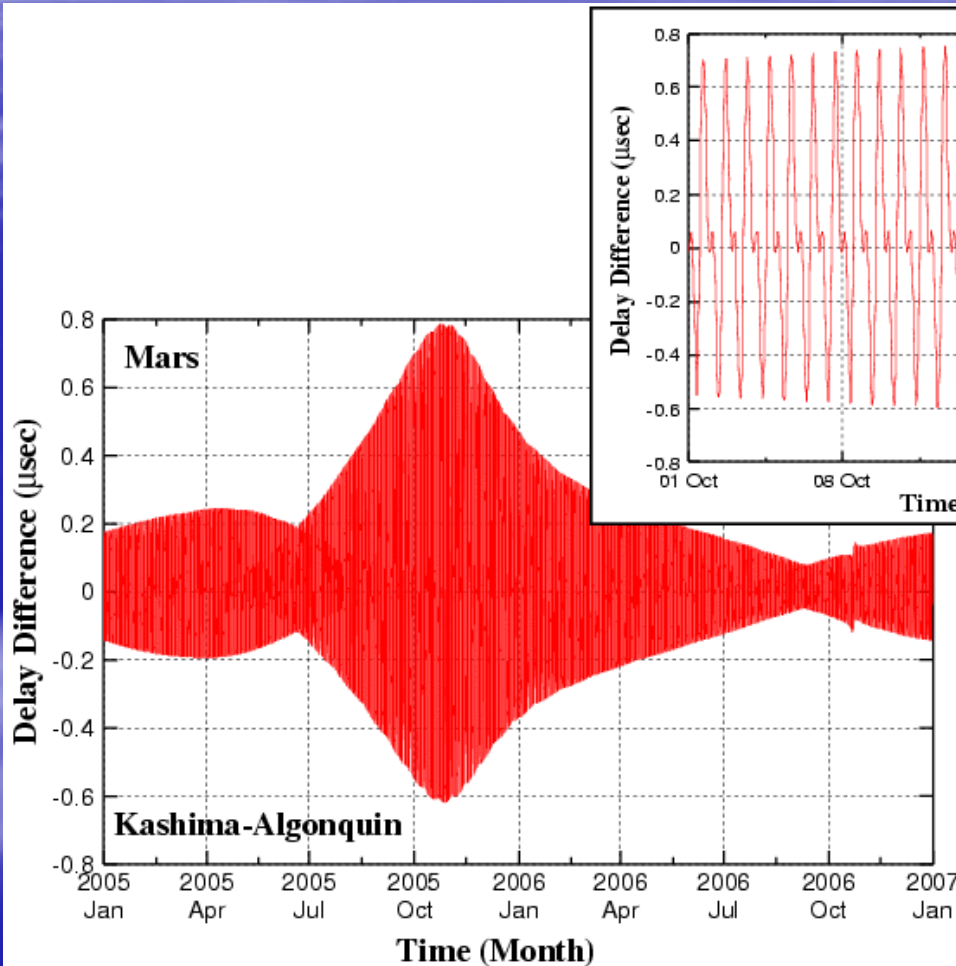
$$\tau_2 - \tau_1 = \frac{\Delta t_g - \frac{\vec{S} \cdot \vec{b}}{c} \left[1 - (1 + \gamma)U - \frac{V_e^2 + 2\vec{V}_e \cdot \vec{w}_2}{2c^2} \right] - \frac{\vec{V}_e \cdot \vec{b}}{c^2} \left(1 + \frac{\vec{S} \cdot \vec{V}_e}{2c} \right)}{1 + \frac{\vec{S} \cdot (\vec{V}_e + \vec{w}_2)}{c}}$$

Finite Distance VLBI MODEL (Sekido & Fukushima 2005)

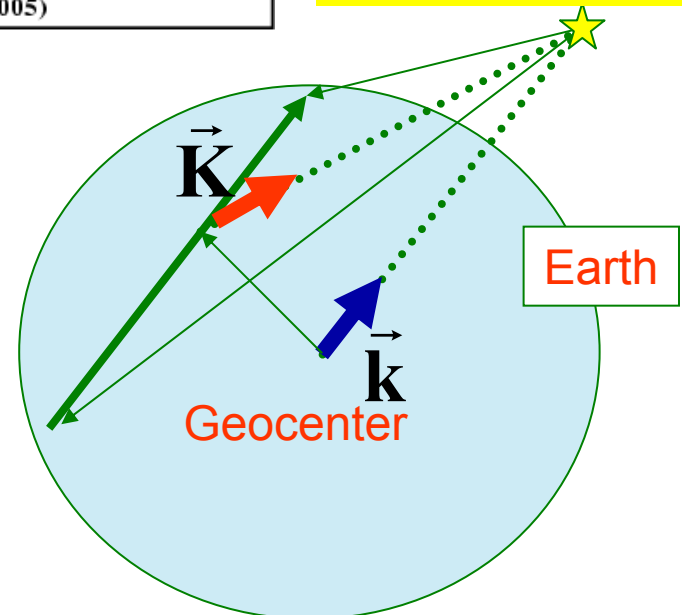
$$\tau_2 - \tau_1 = \frac{\Delta t_g - \frac{\vec{K} \cdot \vec{b}}{c} \left[1 - (1 + \gamma)U - \frac{V_e^2 + 2\vec{V}_e \cdot \vec{w}_2}{2c^2} \right] - \frac{\vec{V}_e \cdot \vec{b}}{c^2} \left(1 + \vec{R}_{02} \cdot \frac{\vec{V}_2}{c} - \frac{\vec{K} \cdot (\vec{V}_e + 2\vec{w}_2)}{2c} \right)}{\left(1 + \vec{R}_{02} \cdot \frac{\vec{V}_2}{c} \right) \left[1 + \frac{\vec{K} \cdot \vec{B} (\beta_2^2 - \beta_{02}^2)}{2R_{02} (1 + \beta_{02})^2} \right]}$$

FVLBI – Consensus model

Mars: Kashima-Algonquin(9000km)

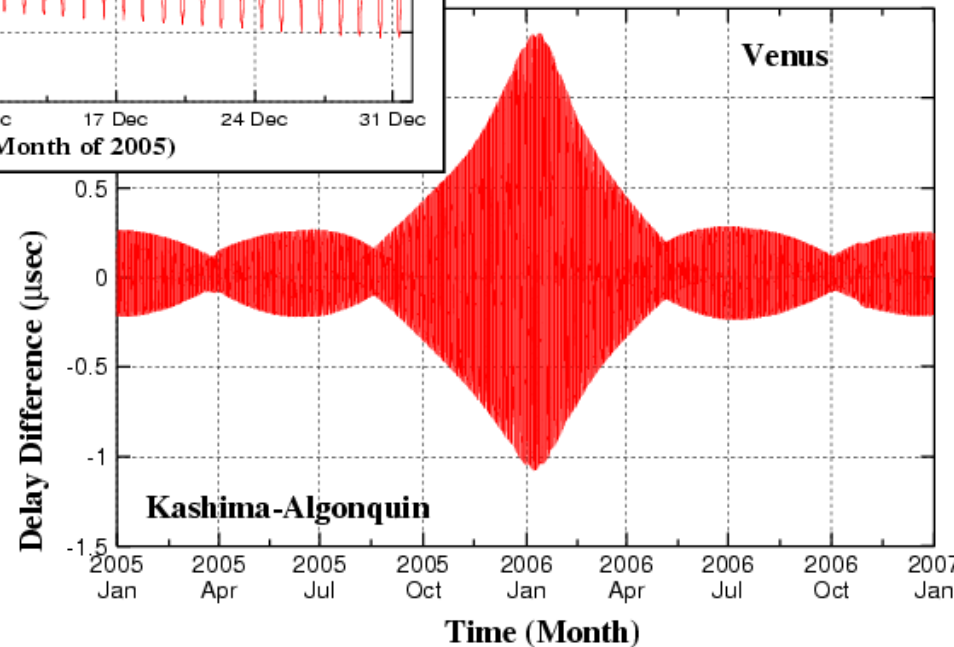
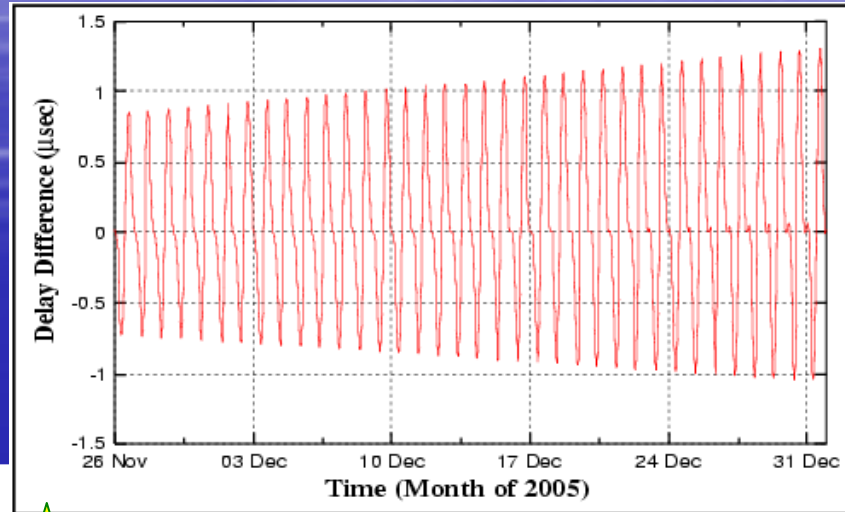


Horizontal Parallax

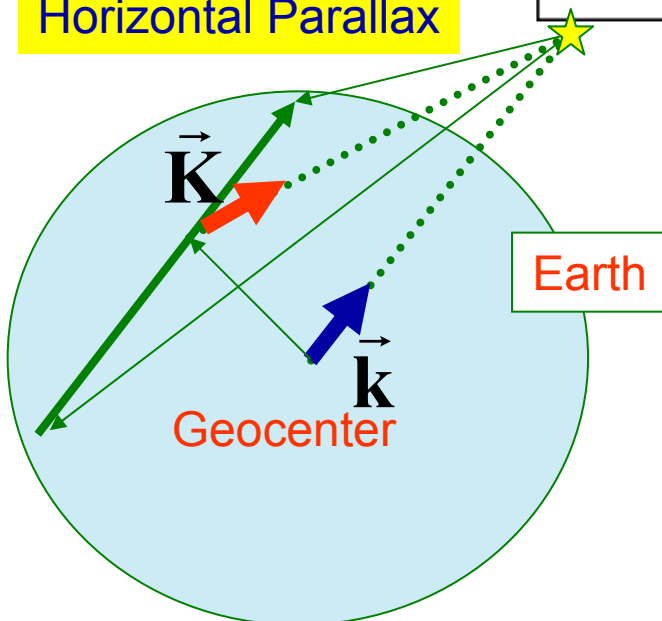


FVLBI – Consensus model

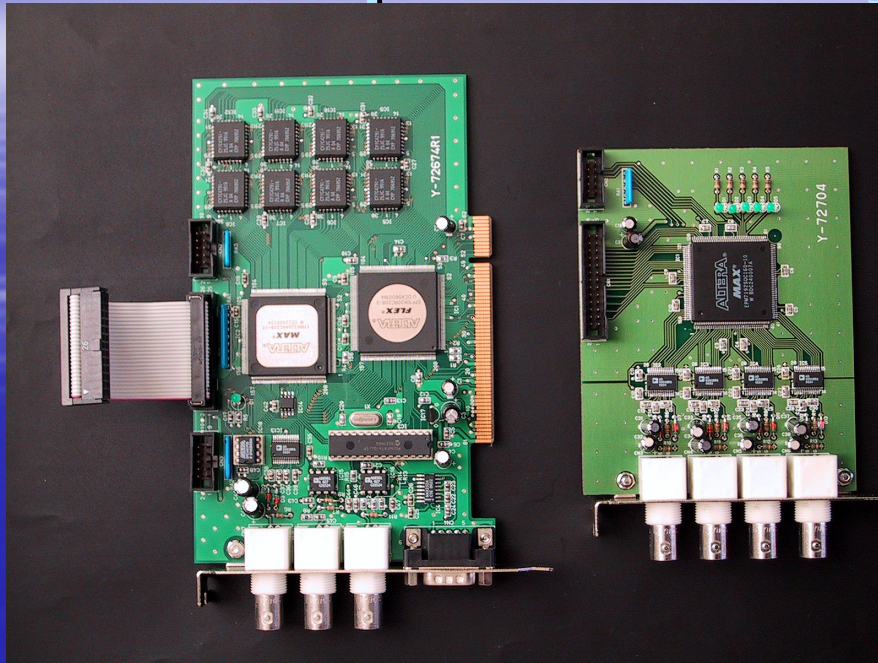
Venus: Kashima-Algonquin(9000km)



Horizontal Parallax



Data Acquisition System: K5/VSSP



K5 VLBI System

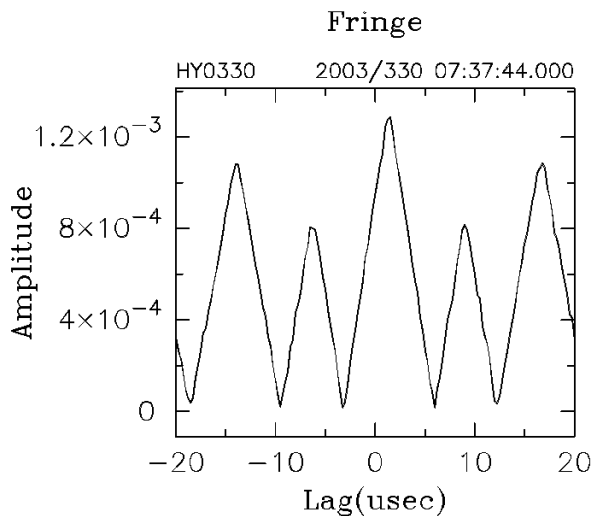
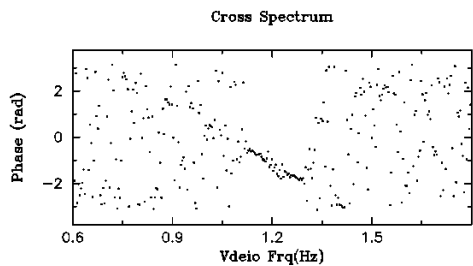
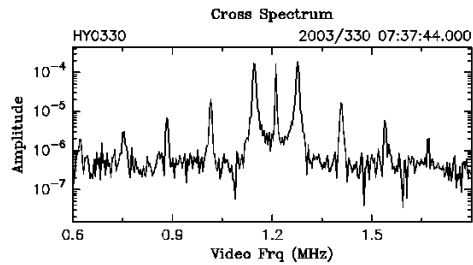
- Sampling rate: 40k-16MHz
- Quantization bit: 1-8bit
- 4ch/board
- 10MHz, 1PPS inputs
- Max rate: 64Mbps/board



Observable: Group Delay

Telemetry Signal

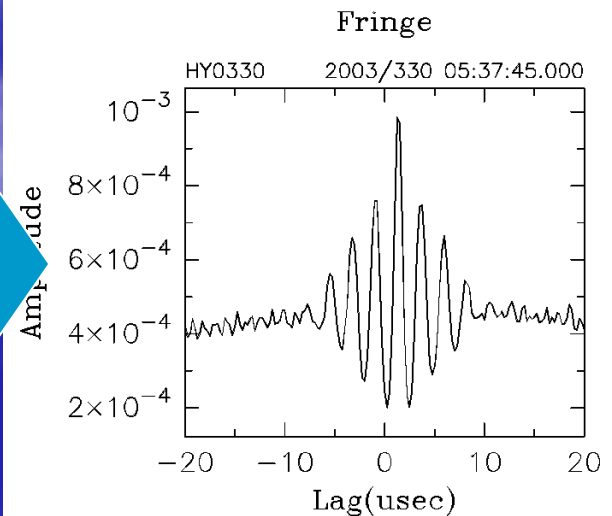
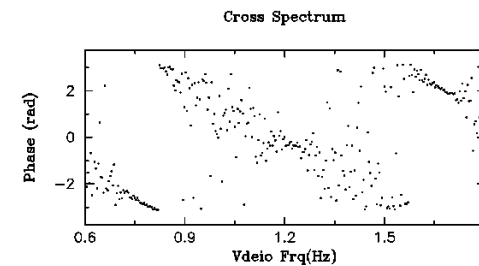
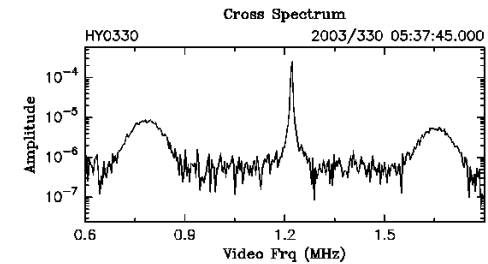
Range signal



Spectrum

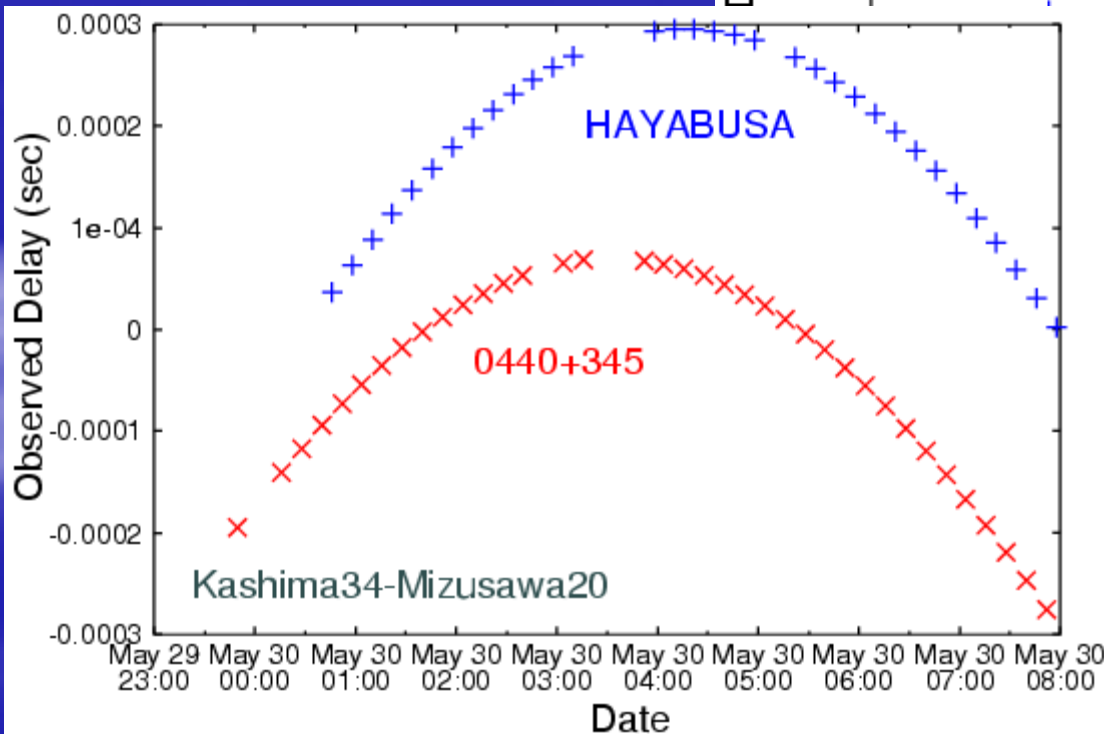
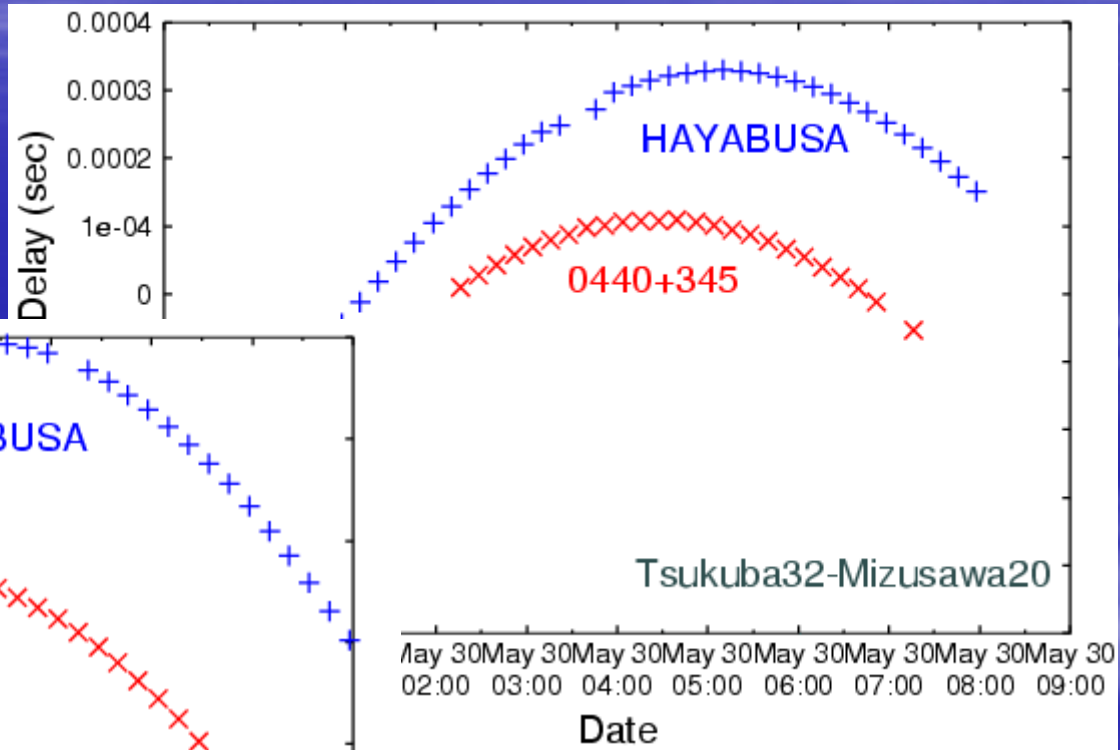
Fringe Phase

Delay Resolution Function

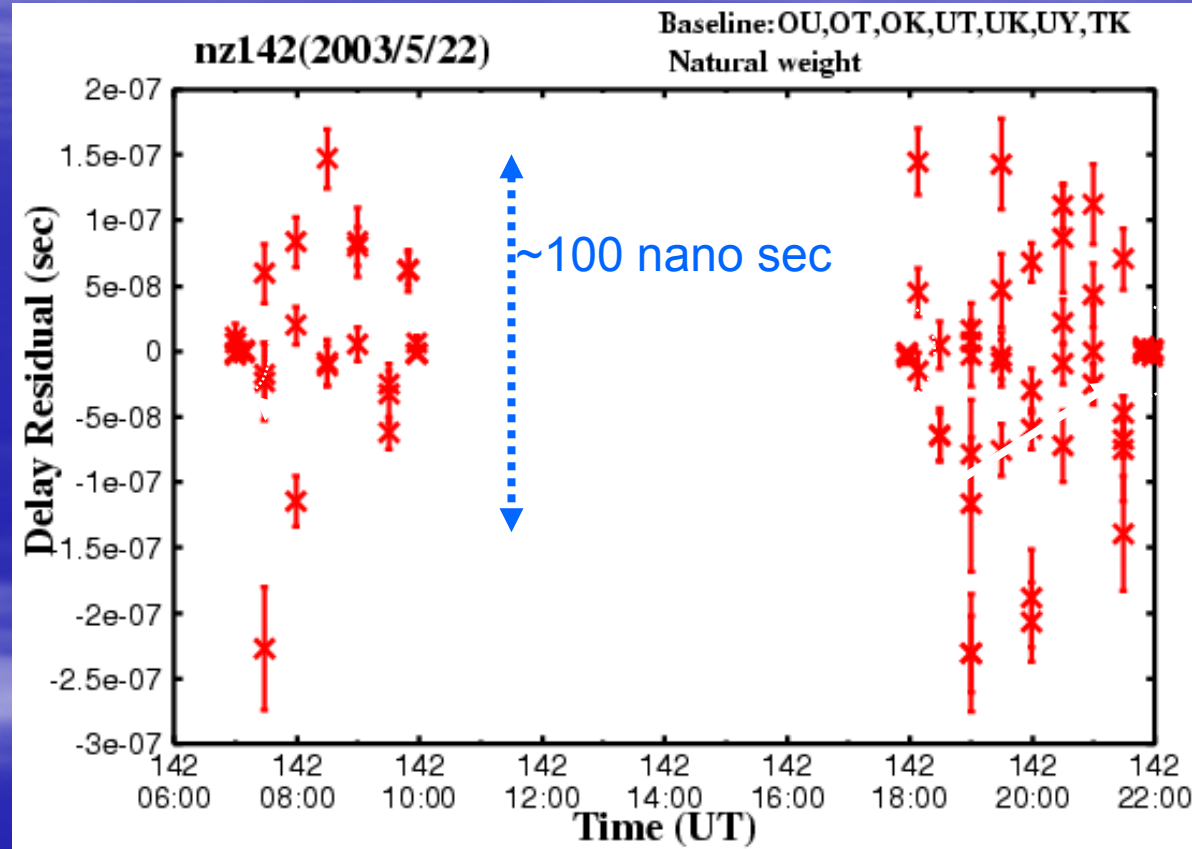
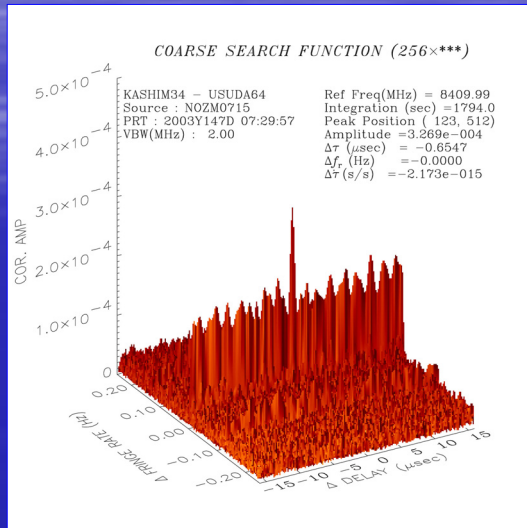
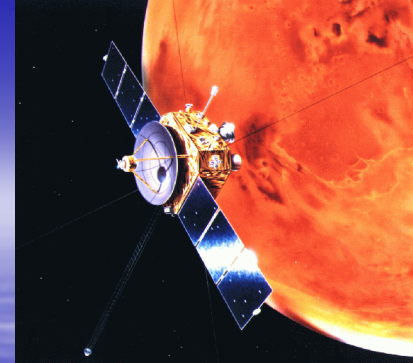


Group Delay: Delta-VLBI

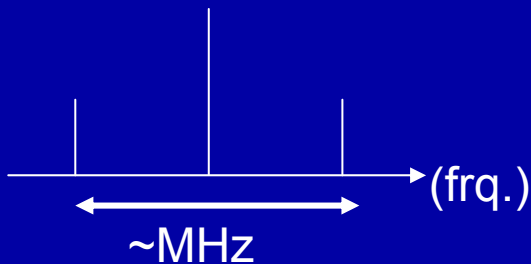
May 30 2005
Spacecraft: HAYABUSA
0440+345: 14.6 deg. Away
Switching cycle: 12 min.



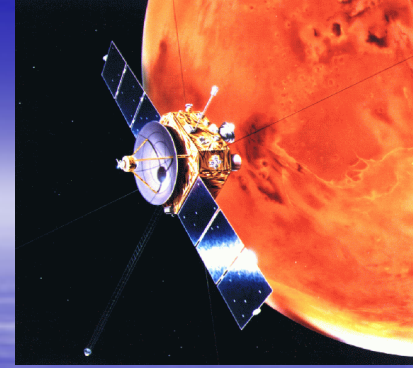
Group Delay (Post-fit Residual) Astrometric Analysis



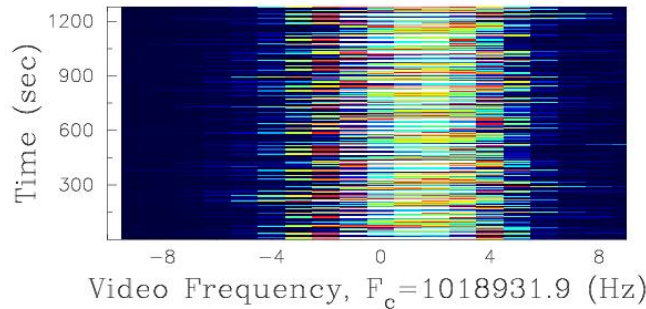
Signal type from Spacecraft



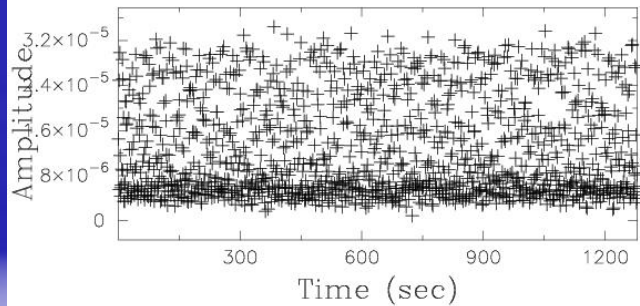
Observable: Phase delay



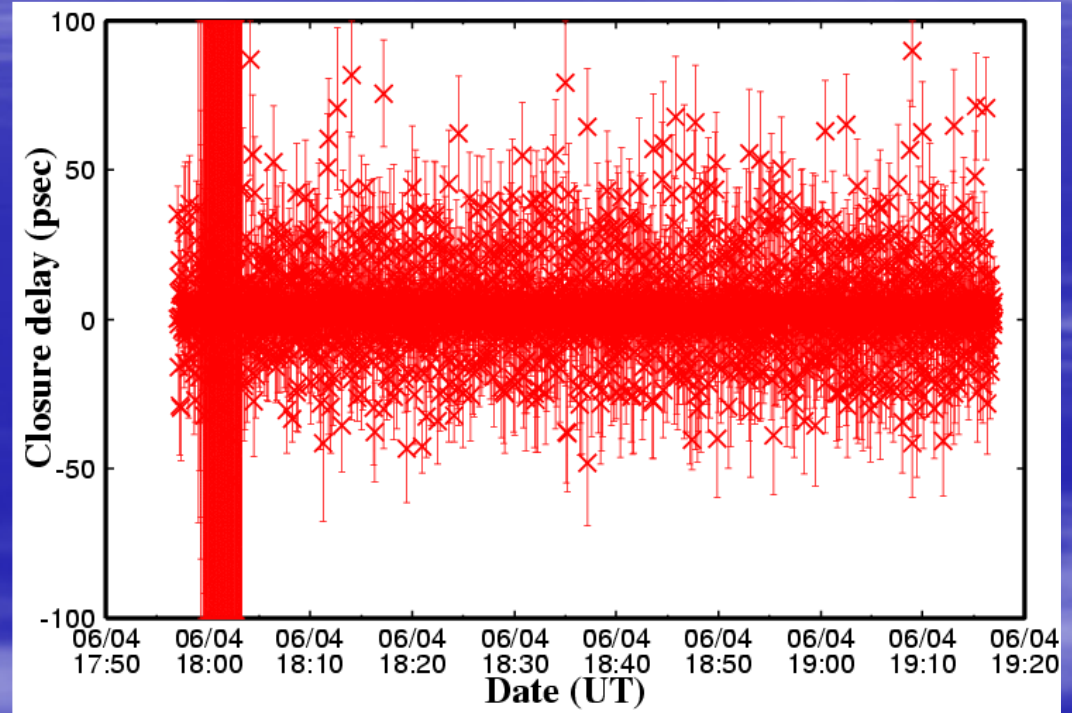
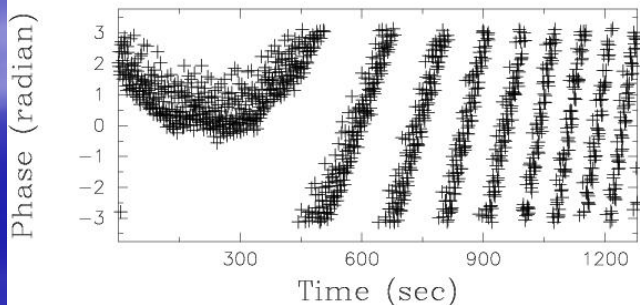
Dynamic Cross Spectrum: Rate Corrected ch=1



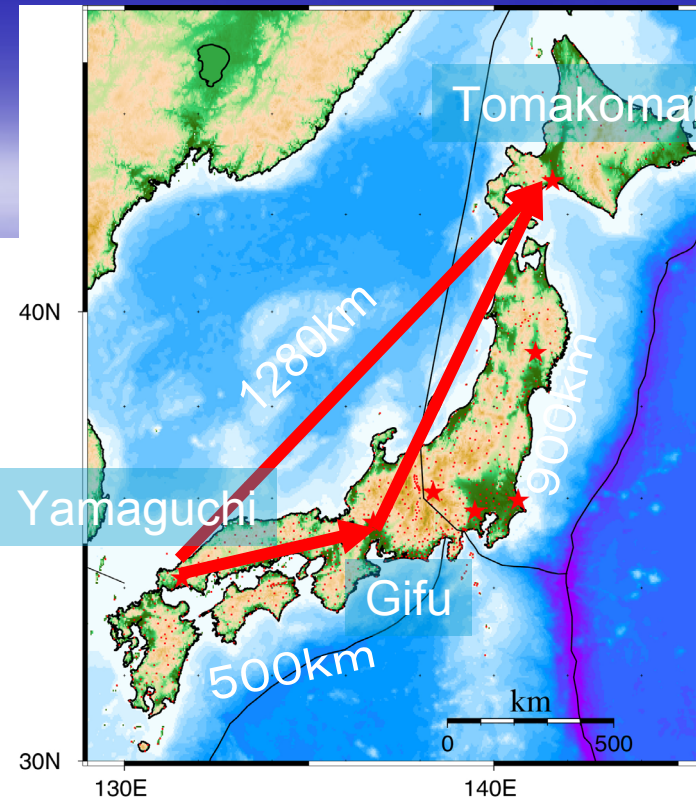
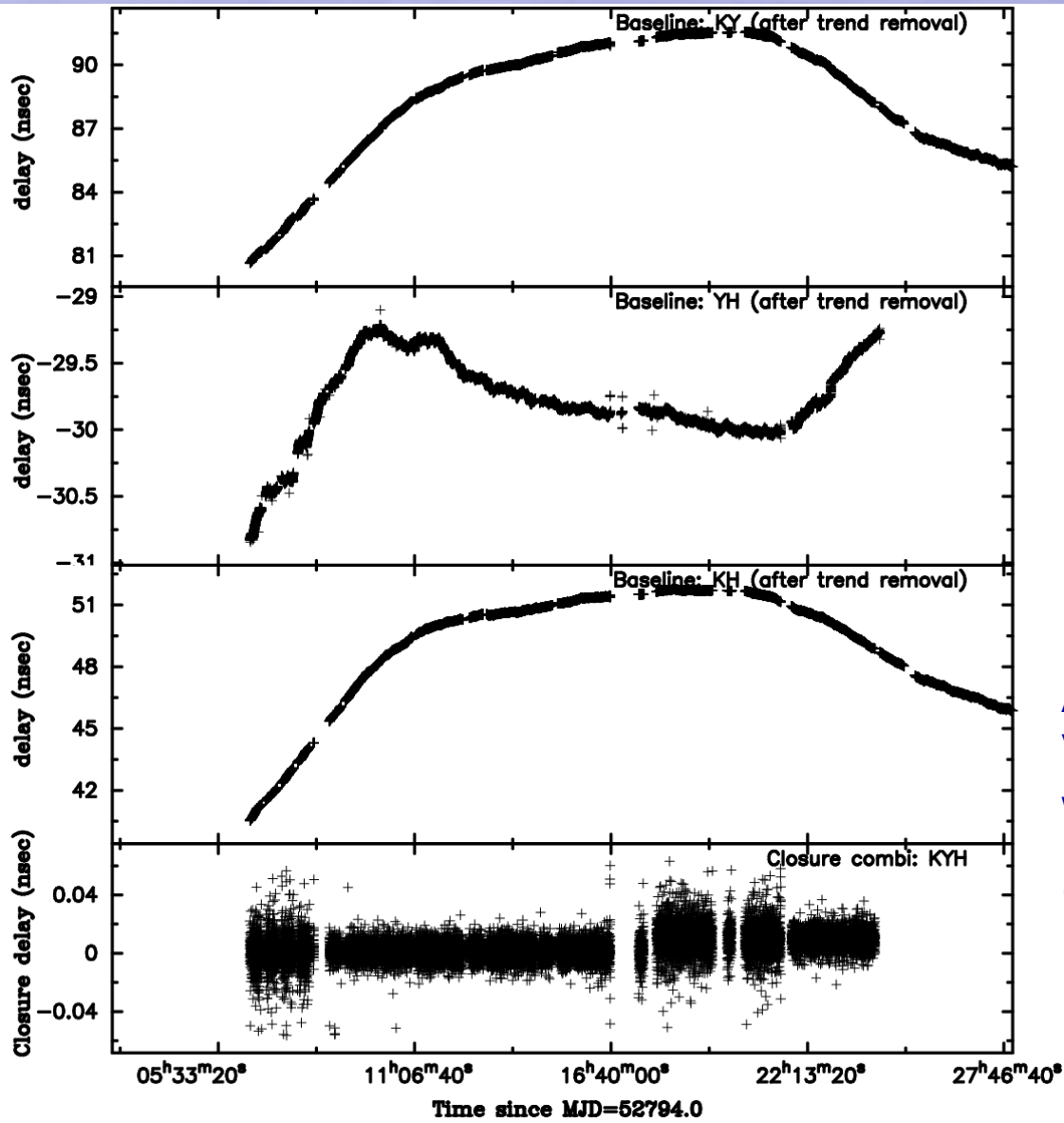
Dynamic Cross Spectrum: Rate Corrected ch=1



Dynamic Cross Spectrum: Rate Corrected ch=1

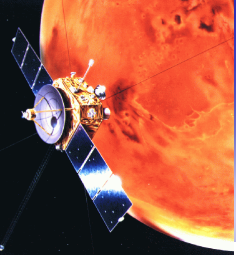


Closure phase delay



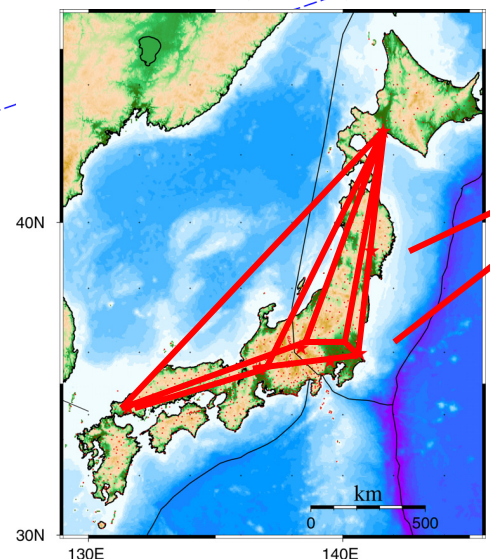
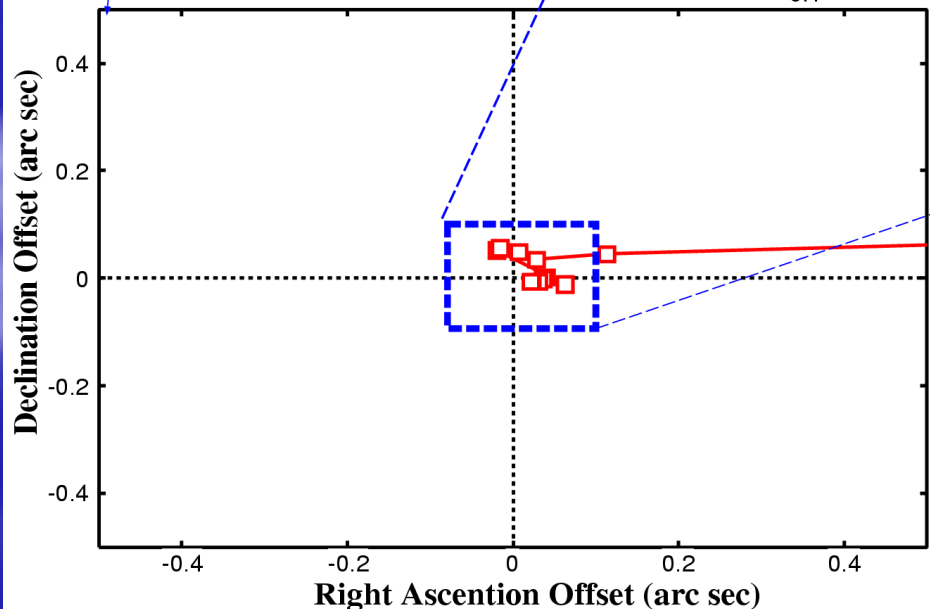
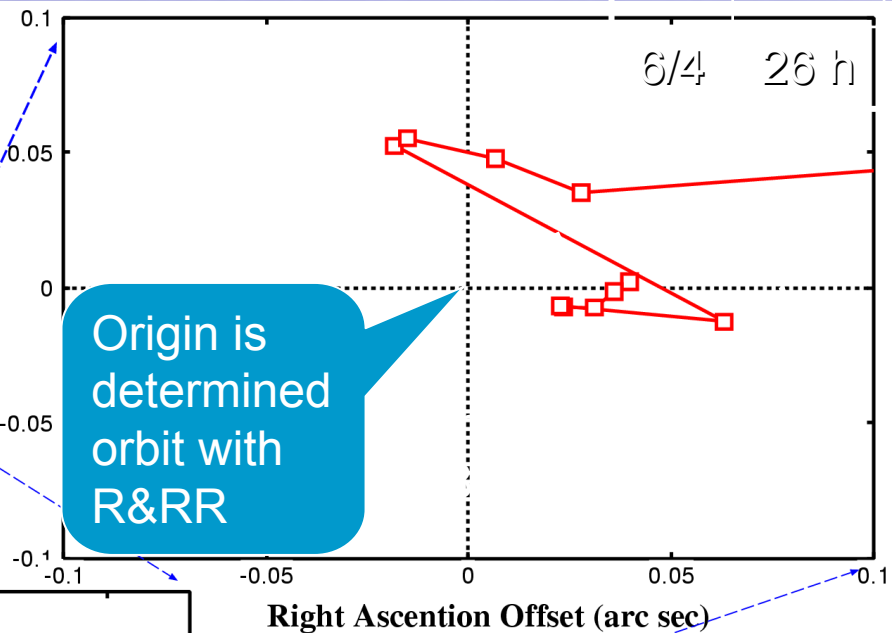
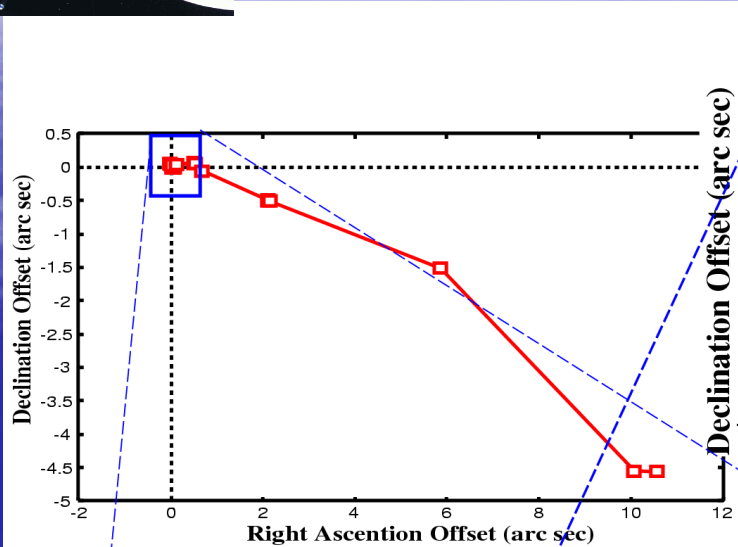
As result of phase connection,
Very precise delay observable
was obtained over 24 hours.

(June 4th experiments)



Radio source coordinates

	Tobs	Nstn	Nbase
	6/4	26 h	7
			21



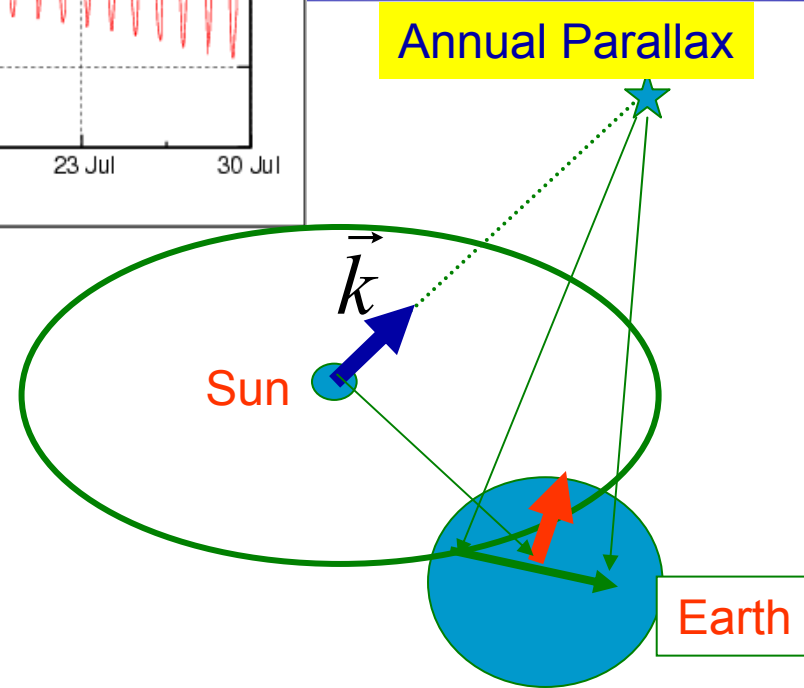
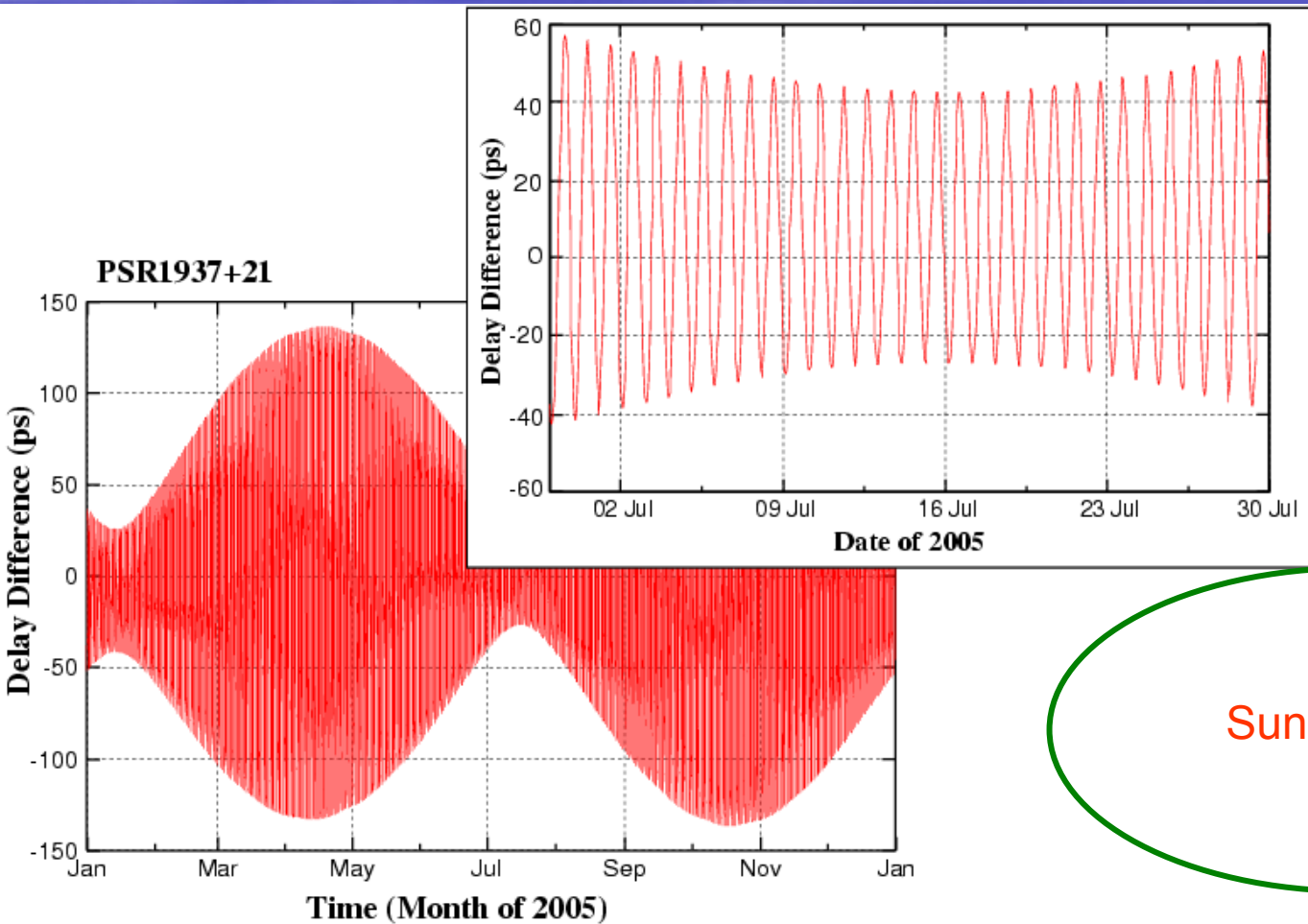
Origin is determined orbit with R&RR

Summary

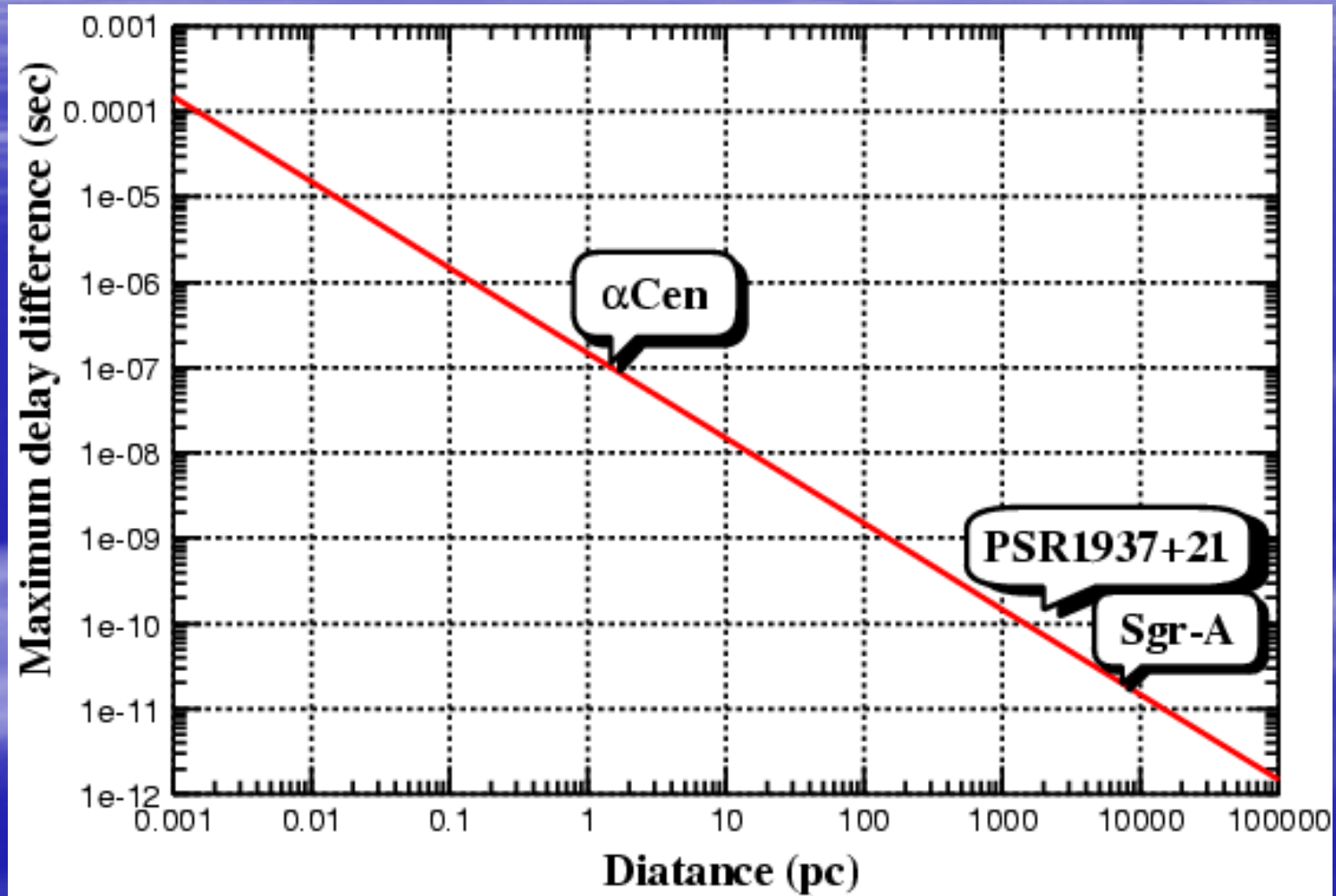
- VLBI delay model for Finite distance Radio Source:
 - Curved wave front = parallax
- Disk-Based Data Recording System + Software Correlator:
 - Network + Flexible Data processing
- Observable:
 - Currently: Delta-VLBI with **Group Delay**
 - Future: Delta-VLBI with **Phase delay**

FVLBI – Consensus model

PSR1937+21: Kashima-Algonquin(9000km)



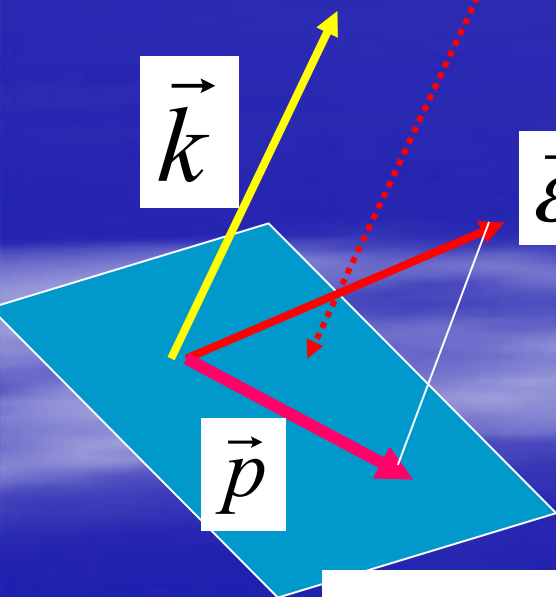
Delay effect by Annual parallax



有限距離モデル—Consensus

距離 $\geq 10\text{pc}$

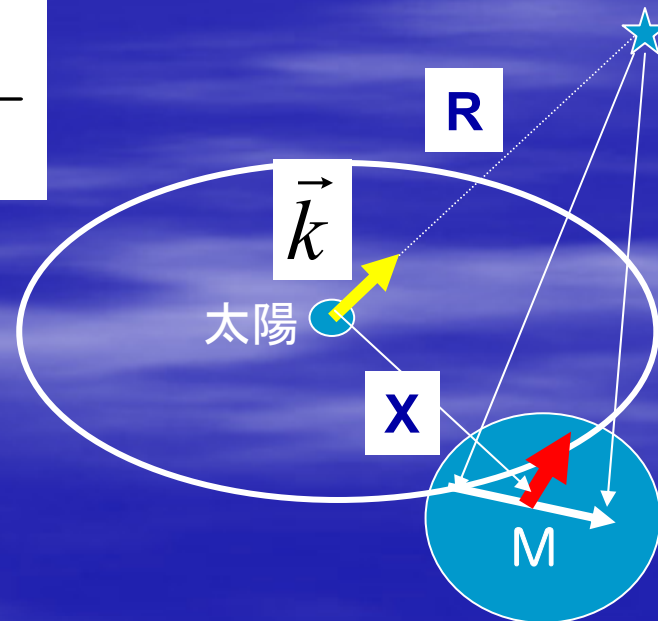
$$\Delta\tau = \frac{\vec{b}}{c} \cdot \vec{p} + \frac{\vec{b} \cdot \vec{k}}{c} \left\{ -[\vec{p} + \vec{k}] \cdot \frac{\vec{V}_2}{c} + \frac{|\vec{V}_2 \times \vec{k}|^2}{2c^2 R_{02}} (\vec{b} \cdot \vec{k}) \right\}$$



視差ベクトル

$$\vec{p} \equiv \vec{\varepsilon} - (\vec{\varepsilon} \cdot \vec{k}) \vec{k}$$

$$\vec{\varepsilon} = \frac{\vec{X}}{R}$$



地球